



Course Title: Soil Mechanics (1)  
Date: 1 June 2016 (Second term)

Course Code: CSE2208  
Allowed time: 1 hrs

Year: 2<sup>nd</sup> Civil Eng.  
No. of Pages: (6)

- SOLVE the following Four questions
- Assume any missing data

**Question Number (1) (13 Points)**

a) The grain size distribution curves of two different soils are shown in Figure (1). It is required to:

- Estimate the effective diameter, the uniformity coefficient, and the coefficient of gradation of both soils.  $D_{10}$   $C_u$   $C_c$  (2 Point)
- Determine the percentages of the different components of each soil. Assuming Unified Soil Classification System (2 Point)
- Classify the two soils (2 points)

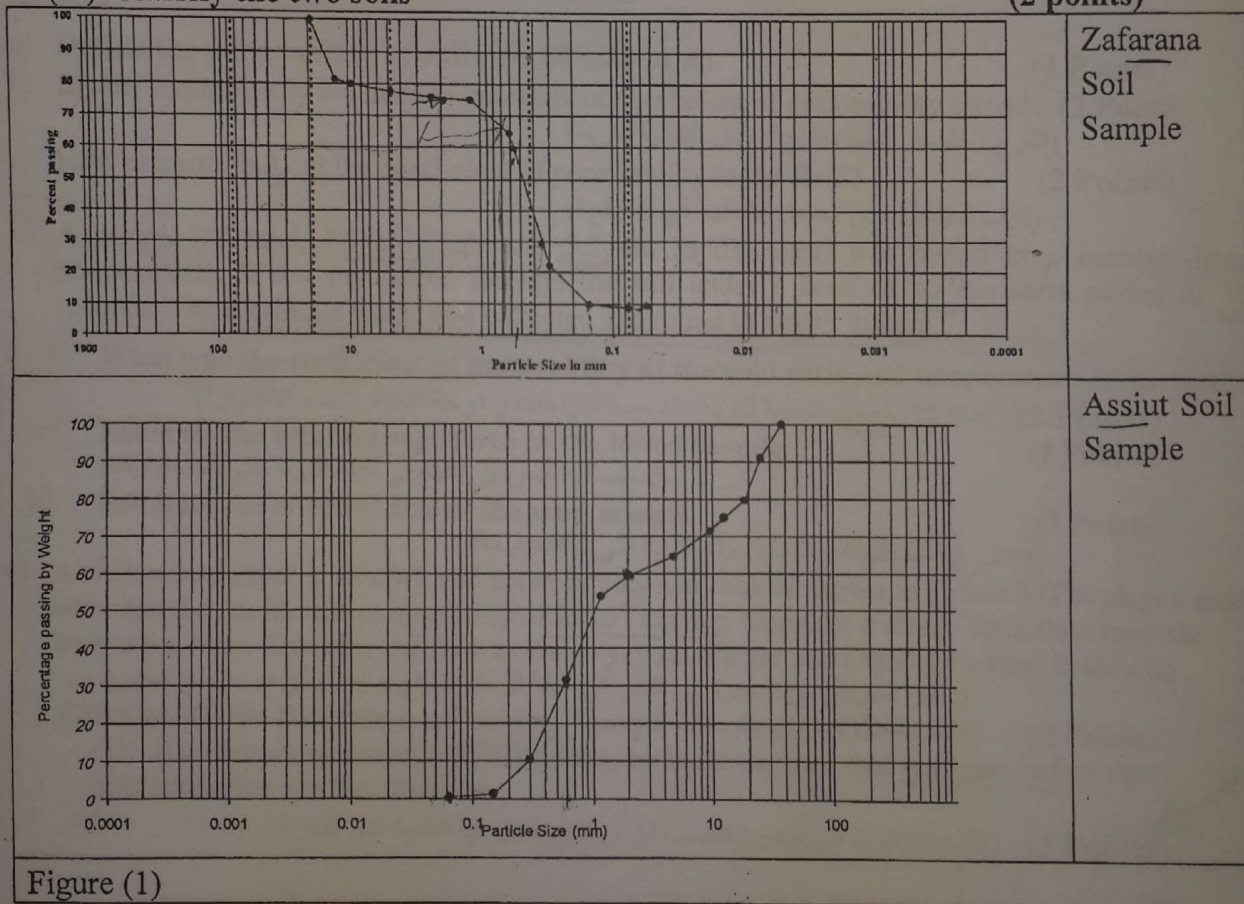


Figure (1)

b) The Atterberg Limits results of soil sample from the Casagrande Cup and Plasticity tests are given in Figure (2). Two determinations for the plastic limit gave water contents of 20.3% and 20.8%.

Determine the following

(I) the liquid limit of the sample (1 point)

(II) the Plastic limit of the sample (1 point)

(III) The activity of the sample if Clay Fraction is 35% (1 point)

(IV) The Liquidity Index of the sample if the natural water content is 25 % (1 point)

(V) The classification of the soil according to the Unified Soil Classification System (1 point)

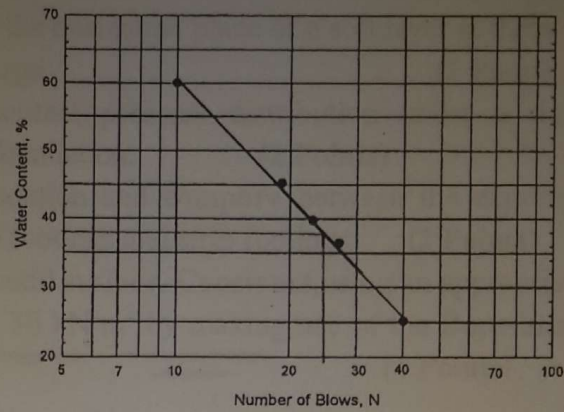


Figure (2)

(VI) The void ratio corresponding to liquid limit if specific gravity is 2.70. (2 points)

**Question Number (2) (15 Points)**

a) Define the permeability of soils. (عرف نفاذية التربة) (1 Points)

b) Briefly explain why we need to know about coefficient of permeability of soils. (إشرح باختصار لماذا نحتاج لمعامل النفاذية للتربة) (2 Points)

c) How can you find out the coefficient of permeability in the field? (كيف نحصل على معامل النفاذية في الموقع؟) (2 Points)

d) A sample of sand, 15 cm high and 5.5 cm in diameter, was tested in a constant-head permeameter. Water percolated through the soil under a head of 45 cm for a period of 10 seconds. The discharge water was collected and found to weigh 800 gm. (2 Points)

i. What was the coefficient of permeability at the void ratio and temperature of the test? (ماذا كان معامل النفاذية للتربة عند نسبة الفراغات و درجة الحرارة أثناء الاختبار؟) (2 Points)

ii. Estimate the total seepage force in the tested sample (احسب قوة السريان الكلية في عينة التربة التي تم اختبارها) (2 Points)

iii. Estimate the effective size of the sand sample. (احسب المقاس الفعال لعينة التربة التي تم اختبارها) (1 Points)

e) A clayey sand layer is sandwiched between clay and rock as shown in Figure 3. The clayey sand layer has the coefficient permeability of  $2 \times 10^{-5}$  cm/sec. Consider a steady state flow from the lake to the river. Consider the flow in the clayey sand layer and neglect the flow in the clay. (اعتبر السريان من البحيرة إلى النهر في طبقة الرمل الطيني و إهمل أي سريان في الطين) (2 Points)

Calculate (I) the flow rate in  $m^3/day/m$ . (احسب معدل السريان بالوحدات الموضحة) (2 Points)

(II) If contamination occurred in the lake, estimate the time that will pass before the contamination reaches the river.

(إذا حدث تلوث في البحيرة فاحسب الزمن الذي يصل فيه التلوث إلى النهر) (3 Points)

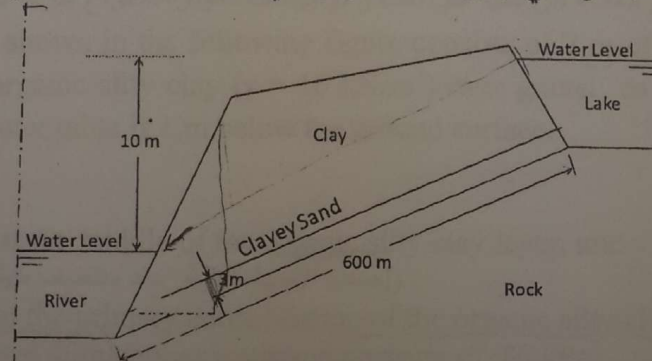


Figure (3)

$$\frac{Q}{t} = k i A =$$

$$k \frac{h}{L} \times A$$



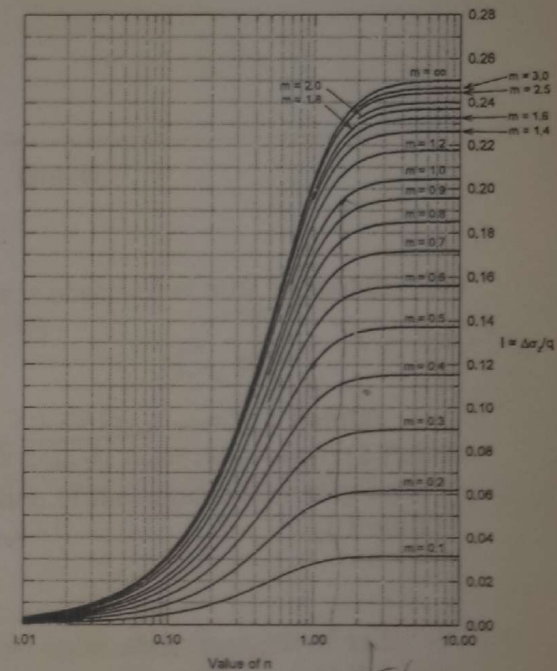
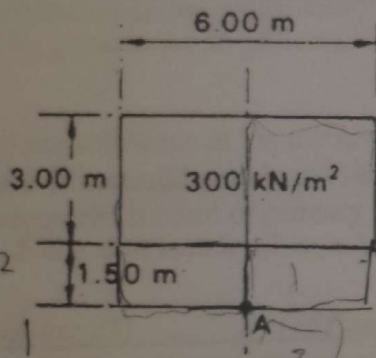
$$+6 + 0.144r^2 = 1 \quad 0.576 = \frac{1}{1+r^2} \quad 0.796 = \frac{1}{1+r^2}$$

### Question Number (3)

(14 Points)

- Draw the variation of vertical stress in the horizontal plane of a soil layer at three different depths below a surface surcharge. (1 Point)
- Draw the shape of the expected contact pressure distribution under a rigid foundation as well as under a flexible foundation. (2 Points)
- Define the pressure bulb under a foundation and compare between the expected sizes of the pressure bulb below square footings and strip footings. (2 Points)
- A point load of 1000 kN acts at the ground surface. Construct, using an appropriate scale, the isobar for a value of  $\Delta\sigma_v = 30 \text{ kN/m}^2$  by making use of the Boussinesq equation. (4 Points)

- A rectangular foundation 6x3m carries uniform pressure of 300 kPa near the surface of a soil mass Figure (4). Determine the vertical stress at a depth of 3m below a point (A) on the center line 1.5 m outside a long edge of the foundation. (5 Points)



### Question Number (4)

(15 Points)

- Briefly explain the fundamental factors influence compressibility of soils. (2 Points)
- Sketch and label the void ratio versus effective stress relationship for (I) Normally consolidated clay and (II) Overconsolidated clay. (2 Points)
- A soil profile shown in the following figure consists of 2 m of sand ( $\gamma = 20 \text{ kN/m}^3$ ) over 6 m of organic silty clay ( $\gamma = 16 \text{ kN/m}^3$ ) over gravel as shown in Figure (5). The ground water table is 1 m below the ground surface.

### Calculate

- effective stress at the middle of the organic silty clay layer, and (2 Points)
- settlement due to the primary consolidation of the organic silty clay layer if a surface tank with diameter 40m applies a surface pressure of 80 kPa. (3 Points)

(احسب الهبوط نتيجة إنضغاط طبقة الطين إذا تم وضع خزان بقطر 40 متر يسبب قيمة إجهاد على سطح الأرض بالقيمة المذكورة بالسؤال)

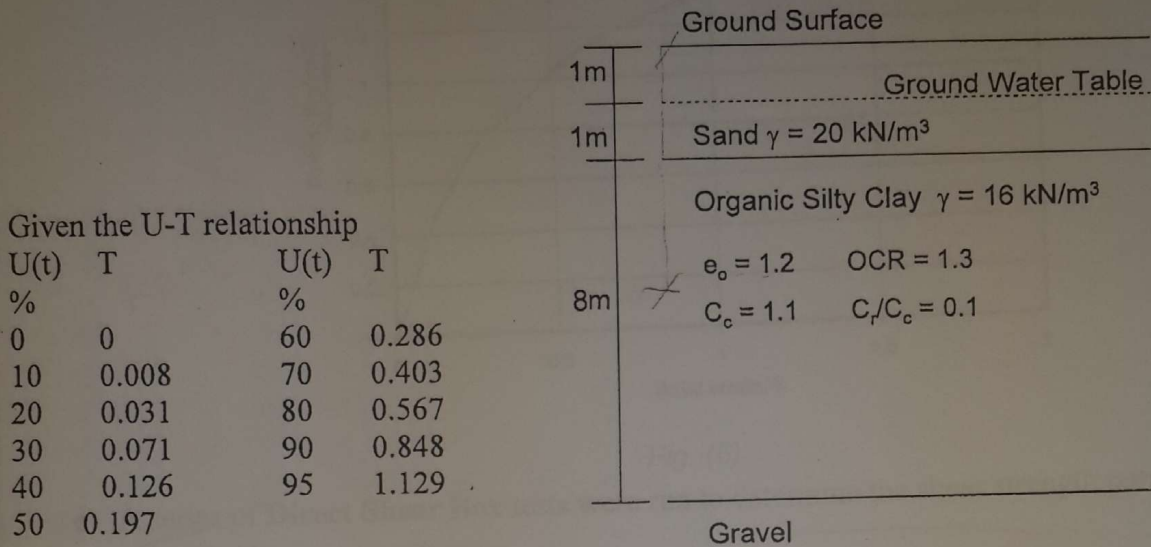


Figure (5)

if 50 cm of settlement of the organic silty clay layer is observed at time 16 months after loading. (إذا تم رصد قيمة هبوط حوالي 50 سم بعد حوالي 16 شهر)

$$C_v = \frac{T_v - \frac{C_v \times t}{H^2}}{H^2}$$

Calculate

- degree of consolidation at the mentioned time, (احسب درجة التصلد) (2 Points)
- coefficient of consolidation in  $m^2/year$ , (احسب معامل التصلد بالوحدات المذكورة) (2 Points)
- the time required for end of primary consolidation of the organic silty clay layer (أحسب الزمن اللازم لحدوث الهبوط نتيجة تصلد طبقة الطين) (2 Points)

### Question Number (5) (18 Points)

- Using clear sketches discuss why we need to know about shear strength of soils. (2 Points)
- Briefly explain the fundamental factors influence shear strength of soils. (2 Points)
- Draw the expected relations between shear stress and shear displacement strain and, also, the expected relation between volumetric change and shear displacement for loose and dense sand samples when tested in a direct shear box apparatus. (2 Points)
- The results of unconfined compression test on blue clay sample are shown in Fig. (6). It is required to:
  - Determine the unconfined compressive strength of the clay. (1 Point)
  - What are the shear strength parameters of the clay sample? (1 Point)
  - Are these parameters, drained or undrained parameters? & Why? (2 Points)

$$C_v = \frac{1}{2H^2} \left[ \frac{1}{1 + \left(\frac{r}{z}\right)^2} \right] \frac{S}{2}$$



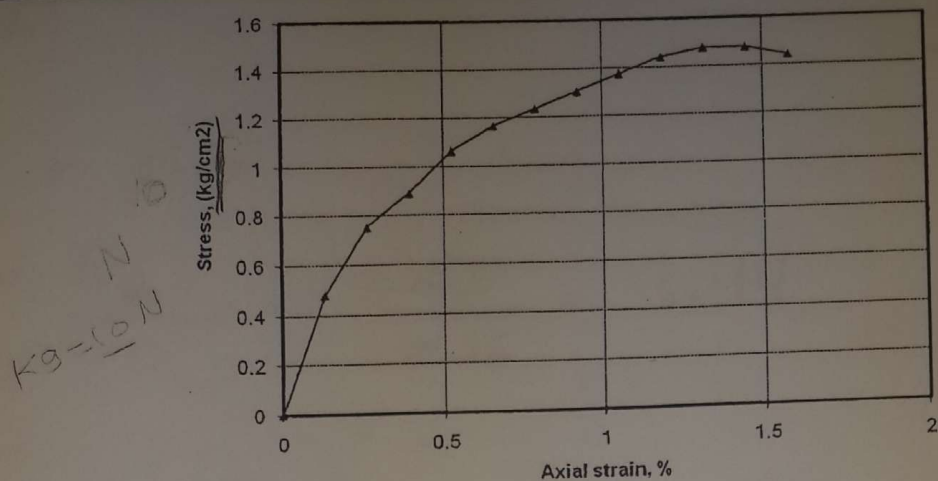


Fig. (6)

- e) A series of **Direct Shear Box** tests were run to determine the shear strength parameters of a soil. The tests results are:

Test No.	Normal Stress $\sigma'$ (kN/m <sup>2</sup> )	Shear Stress at Failure $\tau$ (kN/m <sup>2</sup> )
1	50	33
2	100	51
3	200	88

- Draw** the Mohr Shear strength envelope for the given data. (1 Point)
  - Based on a best-fitted straight line Mohr envelope, **evaluate** the value of  $c'$  and  $\phi'$ . (2 Points)
  - Considering that the same soil was tested in the **triaxial apparatus** and that the same shear strength envelope was developed, if the confining stress ( $\sigma_3$ ) = 40 kN/m<sup>2</sup>, **determine** the maximum axial stress ( $\sigma_1$ ). (3 Points)
- f) A natural slope consists of the same **stiff silty clay** in (e) above (it has the same  $c'$  and  $\phi'$ ). For stability analysis of the slope, **consider one segment** of the failure surface with effective normal stress  $\sigma'_n$  of 40 kN/m<sup>2</sup>. **Calculate** the shear strength of the soil on the segment. (2 Points)

End of questions ..... Best Wishes  
 Prof. Dr. Marawan M. Shahien & the committee

Soil (A)

$$D_{10\%} = 0.16$$

$$C_u = \frac{D_{60\%}}{D_{10\%}} = \frac{0.55}{0.16} = 3.44$$

$$C_g = \frac{D_{60\%} * D_{10\%}}{(D_{30\%})^2} = \frac{0.16 * 0.55}{(0.35)^2} = 1.4$$

Soil (B)

$$D_{10\%} = 0.3$$

$$C_u = \frac{D_{60\%}}{D_{10\%}} = \frac{2}{0.3} = 6.67$$

$$C_g = \frac{D_{60\%} * D_{10\%}}{(D_{30\%})^2} = \frac{2 * 0.3}{(0.6)^2} = 0.6$$

(ii)

Soil (A)

$$\% \text{ gravel} = 100 - 78 = 22\%$$

$$\% \text{ Sand} = 78 - 9 = 69\%$$

$$\% \text{ fines} = 9\%$$

Soil (B)

$$\% \text{ gravel} = 100 - 65 = 35\%$$

$$\% \text{ Sand} = 65\%$$

$$\% \text{ fines} = 0\%$$

(iii)

②

Soil (A)  $\rightarrow$  Poorly graded Sand

Soil (B)  $\rightarrow$  " " "

(b)  $\rightarrow$   $L.L. = 38\%$

$\rightarrow P.L. = \frac{20.3 + 20.8}{2} = 20.55\%$

$\rightarrow A = \frac{P.I.}{\% \text{ Age of Clay}}$

$P.I. = L.L. - P.L. = 38 - 20.55 = 17.45\%$

$A = \frac{17.45}{35} = 0.49 \approx 0.5$

$\rightarrow L.I. = \frac{w_c - P.L.}{L.L. - P.L.} = \frac{25 - 20.55}{38 - 20.55}$   
 $= 0.255$

$\rightarrow$  CL

$\rightarrow w_c * G_s = S * e$

$0.38 * 2.7 = 1 * e$

$\therefore e = 1.03$



(3)

السؤال الثاني :-

$$(d) \quad k = \frac{Q L}{h \cdot A \cdot t}$$

$$k = \frac{800 \times 15}{45 \times \frac{\pi}{4} \times (5.5)^2 \times 10} = 1.12 \text{ cm/sec}$$

$$\rightarrow \text{Seepage Force} = i \gamma_w = \frac{h}{L} \times \gamma_w$$

$$= \frac{45}{15} \times 1 = 3 \text{ ton/m}^3$$

$$k = 1.12 = C \times D_{10\%}^2 = 1 \times D_{10\%}^2$$

$$\therefore D_{10\%} = 1.058 \text{ mm}$$

$$(e) \quad q = k \cdot i \cdot A = 2 \times 10^{-5} \times 10^{-2} \times \frac{10}{600} \times 3 \times 1 \times 60 \times 60 \times 24$$

$$= \frac{3.6 \times 10^{-5} \times 24}{8.64 \times 10^{-4}} \text{ m}^3/\text{day/m}$$



(4)

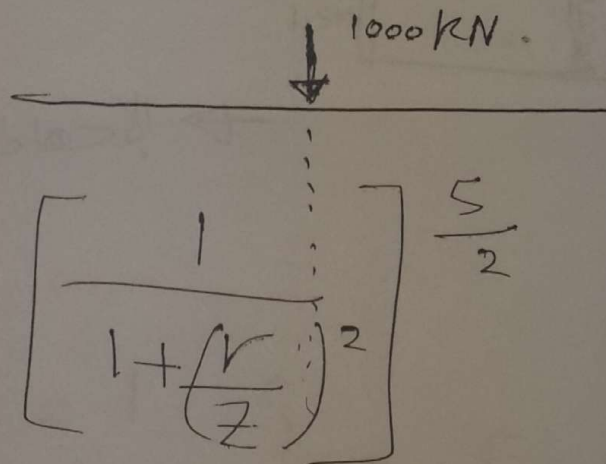
$$V = ki = 2 \times 10^{-5} \times 10^{-2} \times \frac{10}{600} = 3.33 \times 10^{-9} \text{ m/sec}$$

$$V = \frac{L}{t} = 3.33 \times 10^{-9} = \frac{600}{t}$$

$$t = 1.8 \times 10^{11} \text{ sec}$$

السؤال الثالث

(d)



$$\Delta \sigma_v = \frac{3P}{2\pi z^2} \left[ \frac{1}{1 + \left(\frac{r}{z}\right)^2} \right]^{\frac{5}{2}}$$

$$30 = \frac{3 \times 1000}{2\pi \times z^2} \left[ \frac{1}{1 + 0} \right]^{\frac{5}{2}}$$

$$z^2 = 15.9 \text{ m} \rightarrow \text{Pressure Bulb} \quad \text{نطاق الضغط}$$

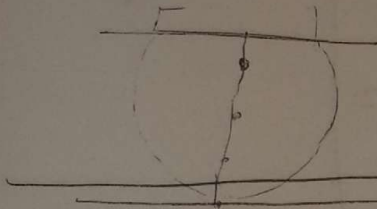
$$\therefore z = 3.99 \text{ m}$$

at  $Z = 1m \rightarrow r = 1.42$

(5)

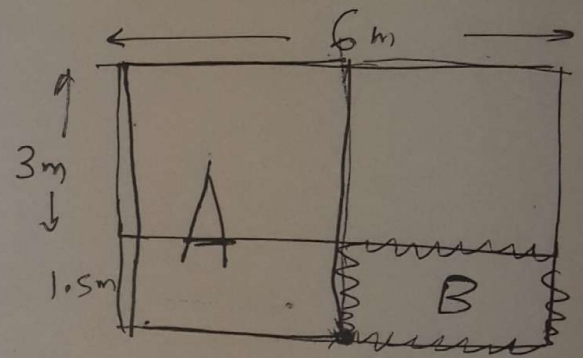
at  $Z = 2m \rightarrow r = 1.72$

$Z = 3m \rightarrow r = 1.52$



← ترسم الـ B. bulb

(e)



← الإحداثيات الناقصة في المساحة (A)  
(4.5 × 3) m

$$m = \frac{x}{z} = \frac{3}{3} = 1$$

$$n = \frac{y}{z} = \frac{4.5}{3} = 1.5$$

}  $\rightarrow I = 0.195$

← الإحداثيات الناقصة في المساحة B ←  
(3 × 1.5)

$$m = \frac{1.5}{3} = 0.5$$

$$n = \frac{3}{3} = 1$$

}  $\rightarrow I = 0.12$



$$\therefore \Delta \sigma_{v(A)} = 2 \left[ 0.195 \times 300 - 0.12 \times 5 \right] \quad (6)$$

$I \times q$

$$= 45 \text{ kN/m}^2$$

Q4

(1)

(C)

$$(i) \sigma'_v = 1 + 20 + 1 + 10 + 4 + 6 = 54 \text{ kN/m}^2$$

$$(ii) \Delta \sigma_v = \frac{q \cdot \frac{\pi}{4} (D)^2}{\frac{\pi}{4} (D+Z)^2}$$
$$= \frac{80 \cdot \frac{\pi}{4} \cdot (40)^2}{\frac{\pi}{4} (40+6)^2} = 60.5 \text{ kN/m}^2$$

$$\text{OCR} = \frac{\sigma_p}{\sigma_{v0}} \quad \sigma_p = 1.3 + 54 = 70.2 \text{ kN}$$

$$\sigma'_p = 54 + 60.5 = 114.5 \text{ kN/m}^2$$

$$S = \frac{c_v \cdot L}{1+e_0} \log\left(\frac{\sigma_p}{\sigma_{v0}}\right) + \frac{c_c \cdot L}{1+e_0} \log\left(\frac{\sigma'_p}{\sigma_{v0}}\right)$$
$$= \frac{0.11 + 8}{1+1.2} \log\left(\frac{70.2}{60.5}\right) + \frac{1.1 + 8}{1+1.2} \log\left(\frac{114.5}{70.2}\right)$$
$$= 0.876 \text{ m} = 87.6 \text{ cm}$$



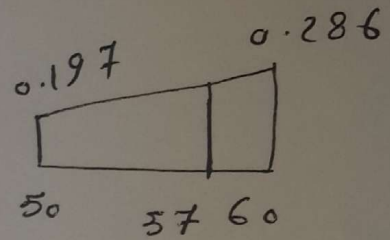
(2)

(iii)  $t = 16 \text{ months} \Rightarrow S = 50 \text{ cm}$

$$u = \frac{St}{S_f} = \frac{50}{87.6} \times 100 = 57\%$$

(iv)

$$T_v = 0.197 + (0.286 - 0.197) + \frac{7}{10}$$
$$\approx 0.26$$



$$T_v = \frac{C_v + t}{d^2}$$

$$d = 4 \text{ m}$$

$$0.26 = \frac{C_v + \left(\frac{16}{12}\right)}{(4)^2}$$

$$C_v = 3.12 \text{ m}^2/\text{year}$$

(v)

put  $\rightarrow u = 95\% \Rightarrow T_v = 1.129$

$$T_v = \frac{C_v \cdot t}{d^2}$$

$$1.129 = \frac{3.12 + t}{4^2}$$

$$t = 5.79 \text{ year.}$$

Q5

(d) (i)  $q_{un} = 1.44 \text{ kg/cm}^2$

(ii)  $c_{un} = \frac{q_{un}}{2} = \frac{1.44}{2} = 0.72 \text{ kg/cm}^2$

(iii) undrained

(e)

(i)  $\text{مُتَوَسِّطُ الْقَوَى}$

(ii)  $c = 5 \text{ kN/m}^2$   $\phi = 24^\circ.52'$

(iii)  $\sigma_3 = 40 \text{ kN/m}^2$

$\sigma_1 = 93 \text{ kN/m}^2$

(P)  $\sigma = 40 \text{ kN/m}^2$   $c = 5 \text{ kN/m}^2$

$\phi = 24^\circ.52'$

$\tau = c + \sigma \tan \phi$

$= 5 + 40 \tan(24.52) = 23.6 \text{ kN/m}^2$



Q5  
 (11)

